

Cycle Decomposition Numbers of Graphs

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Abstract

One of the most fundamental problems in graph theory concerns whether a graph G can be decomposed into subgraphs, each of which is isomorphic to a given graph H . This includes such well-known problems as to whether a given graph is 1-factorable, or perhaps has a hamiltonian decomposition. Not all graphs G are H -decomposable, so a natural question is: "How close to being H -decomposable is G ?" This talk will explore one possible response to this question. For a graph H without isolated vertices, the H -decomposition number of G is the minimum number of vertices that must be added (along with the appropriate edges incident with these vertices) to G to produce a graph F , containing G as an induced subgraph, such that F is H -decomposable. Results will be presented where H is a cycle.